

Lecture 6

Comparators, Timers, and Digital Circuits

References

Webster, Ch. 3 (Sec. 3.5, 3.10, 3.14, 3.16).

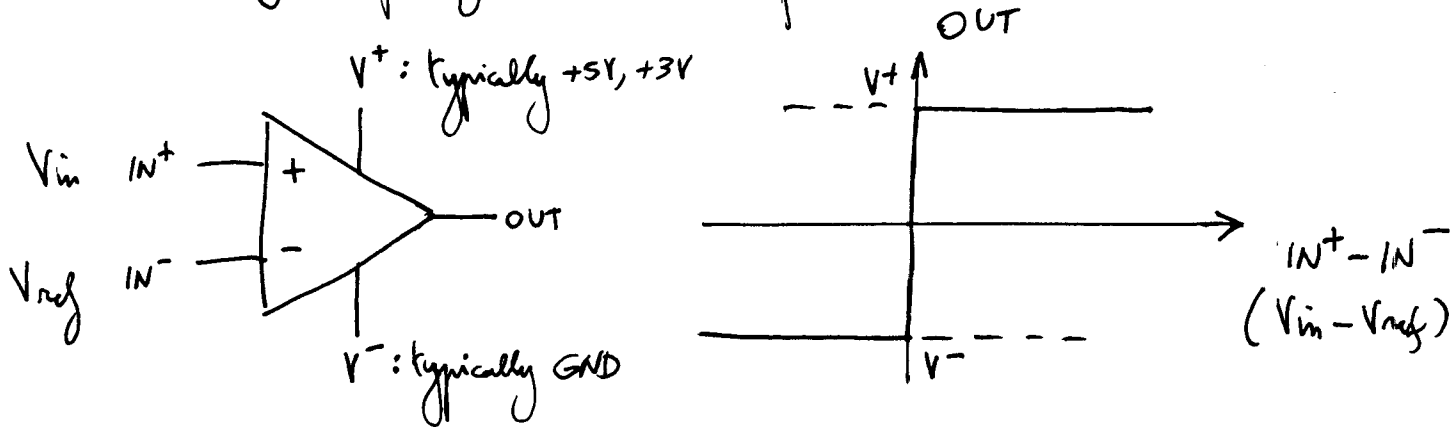
<http://en.wikipedia.org/wiki/Comparator>

http://en.wikipedia.org/wiki/555_timer_IC

http://en.wikipedia.org/wiki/Logic_gates

— Comparators : (Webster Sec. 3.5)

→ Like OP-AMPS, but operate in the SATURATION region rather than the LINEAR region, producing a digital output by comparing the two inputs

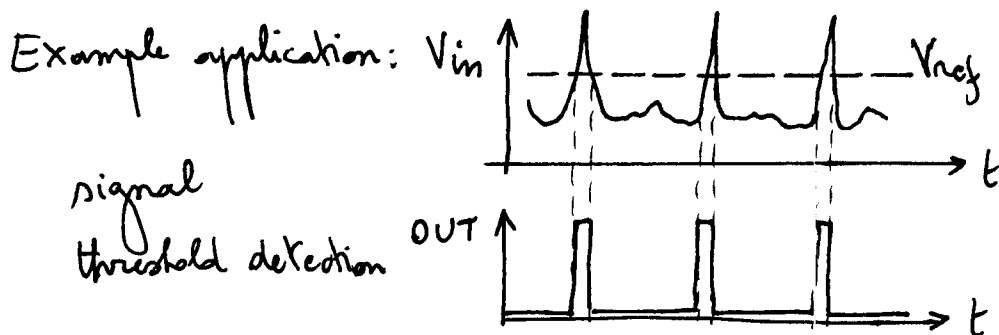
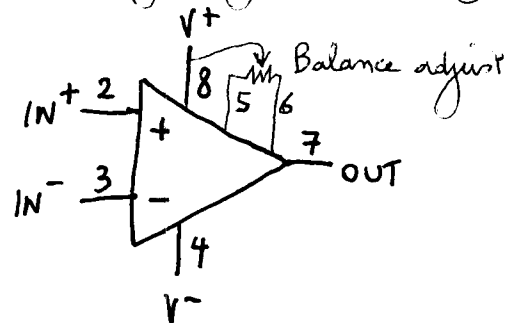


$$OUT = \begin{cases} V^+ & \text{for } IN^+ > IN^- \\ V^- & \text{for } IN^+ < IN^- \end{cases}$$

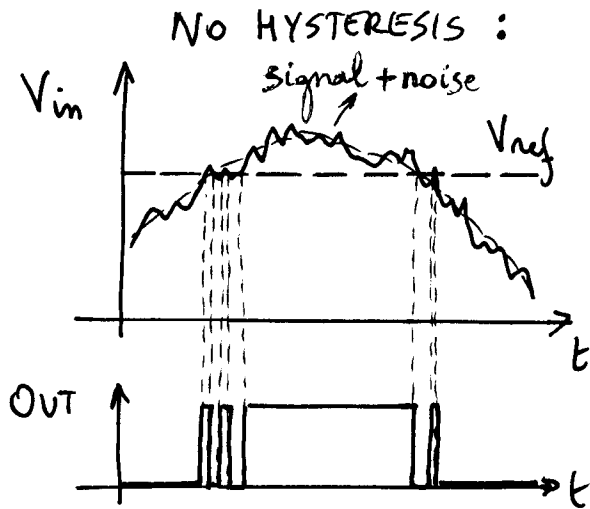
→ Can use a regular op-amp without feedback, although a "real" comparator is better for this purpose (without internal compensation for faster settling)

Typical comparator: LM311

(National Semiconductor, TI)



For good signal threshold detection, it is beneficial to include **HYSTERESIS** in the comparator design:

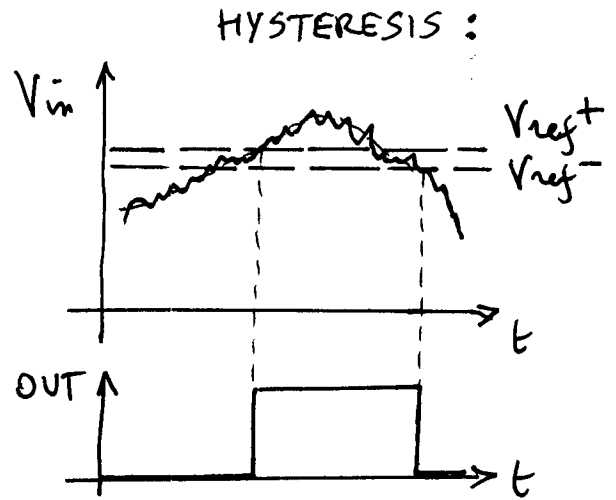
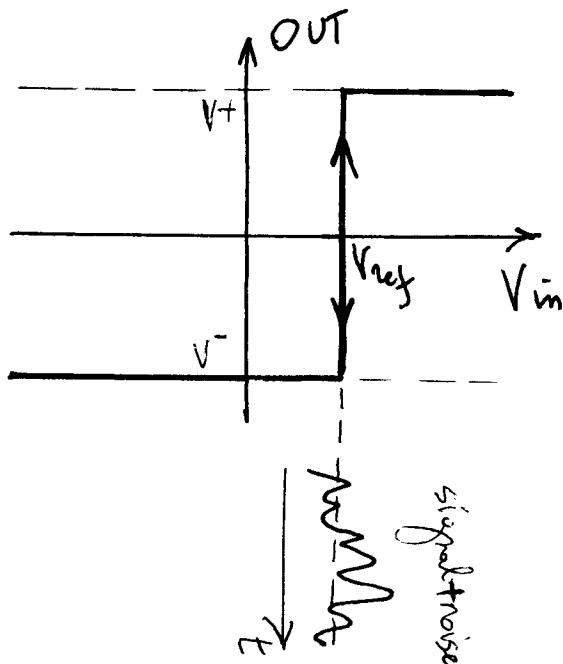


STANDARD COMPARATOR:

single threshold level

$$OUT = \begin{cases} V^+ & \text{when } V_{in} > V_{ref} \\ V^- & \text{when } V_{in} < V_{ref} \end{cases}$$

→ fast, but many erratic transitions



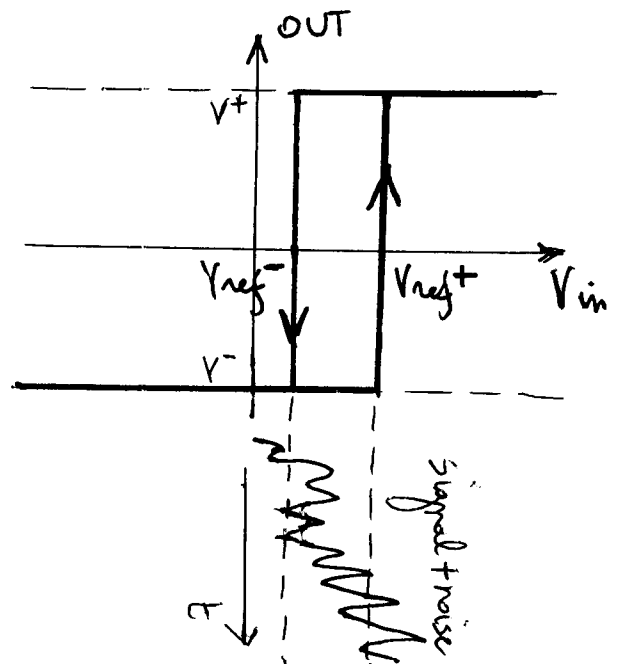
HYSTERETIC COMPARATOR:

two, bistable threshold levels

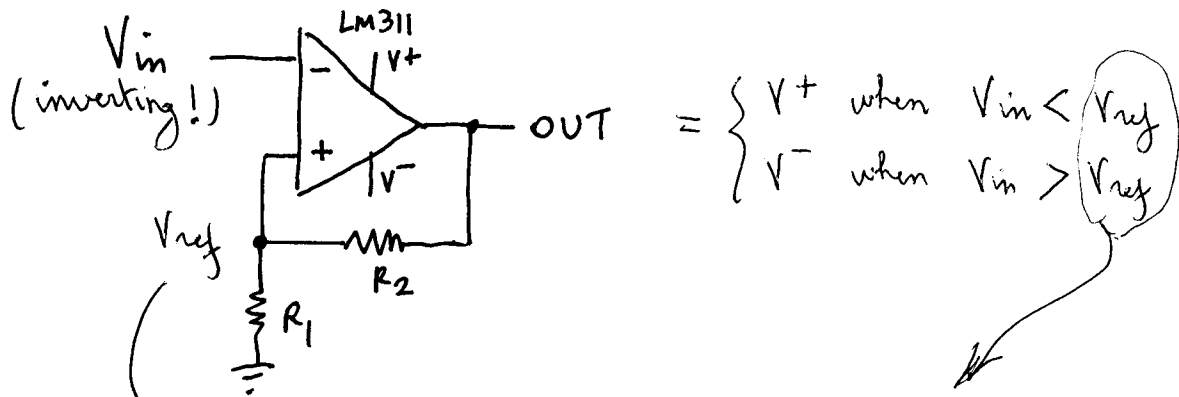
$$OUT \leftarrow V^+ \text{ when } V_{in} > V_{ref}^+ \text{ and } OUT = V^-$$

$$OUT \leftarrow V^- \text{ when } V_{in} < V_{ref}^- \text{ and } OUT = V^+$$

→ reliable, consistent transitions, but delayed response



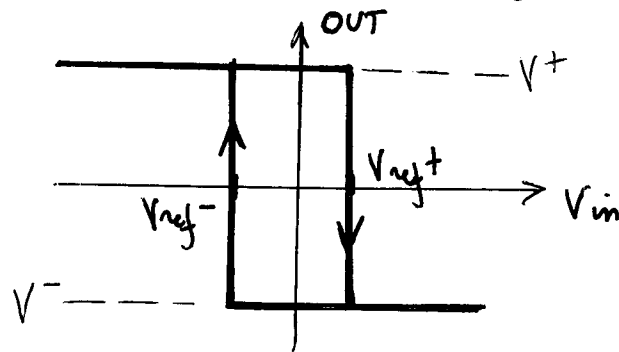
Example: Comparator with positive feedback:



Reference level V_{ref} depends on OUT ! (voltage divider)

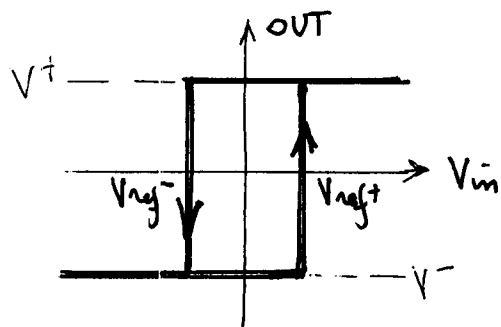
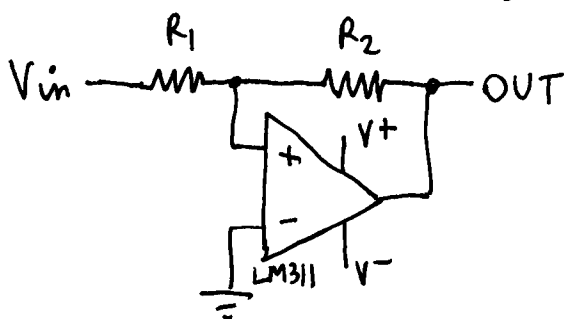
$$OUT = V^- \Rightarrow V_{ref} = V_{ref}^- = \frac{R_1}{R_1 + R_2} \cdot V^-$$

$$OUT = V^+ \Rightarrow V_{ref} = V_{ref}^+ = \frac{R_1}{R_1 + R_2} \cdot V^+$$



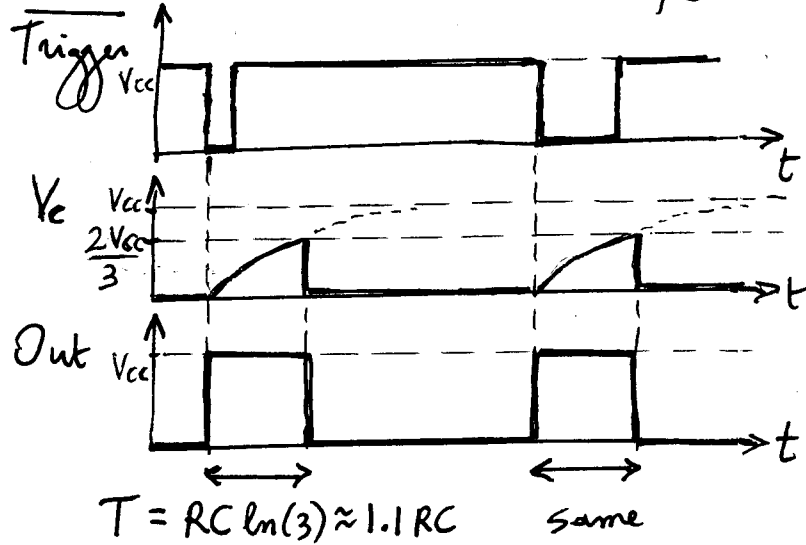
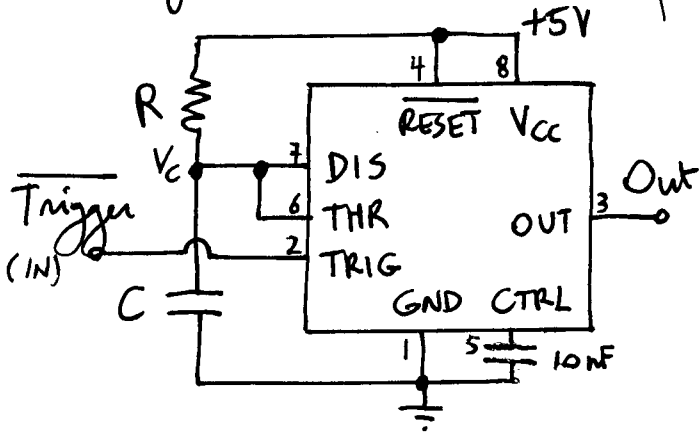
NO HYSTERESIS when $R_1 = 0$, or $R_2 \gg R_1$

Note: this hysteretic comparator is INVERTING. For a NON-INVERTING hysteretic comparator, simply add a digital inverter to invert the polarity of the output, or, e.g.:

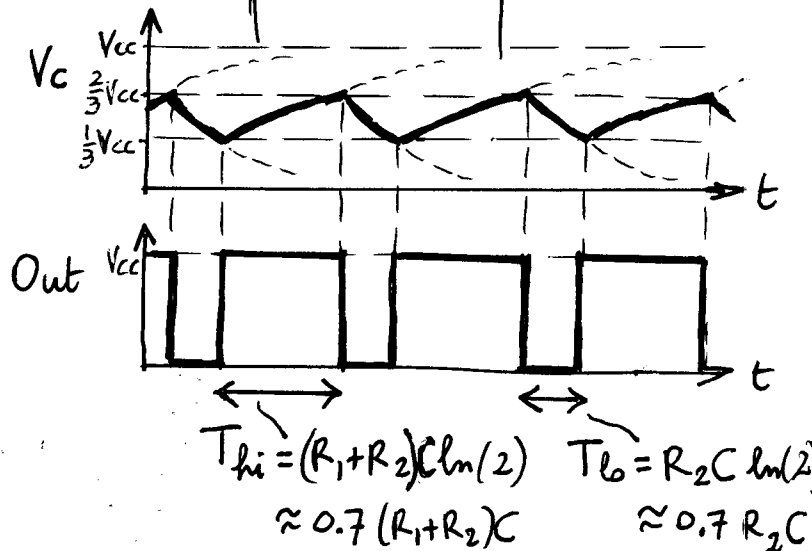
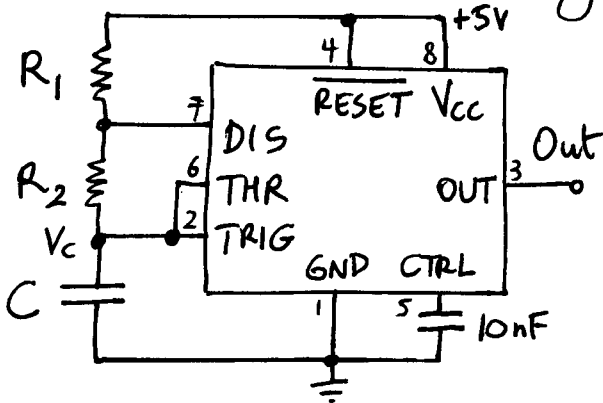


Examples:

- Monostable (single-shot): generates a single pulse of constant width upon a falling edge at the trigger: (downward transition)



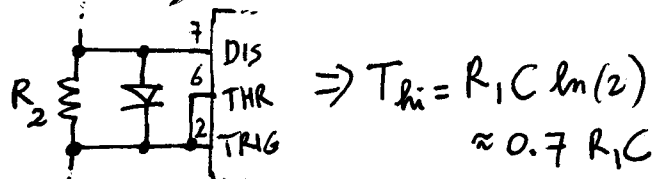
- Astable (oscillator): generates a periodic square wave:



⇒ period $T = T_{lo} + T_{hi} = (R_1 + 2R_2)C \ln(2) \approx 0.7(R_1 + 2R_2)C$

NOTE: Duty cycle > 0.5! ($T_{hi} > T_{lo}$)

FIX for any duty cycle: add diode across R_2



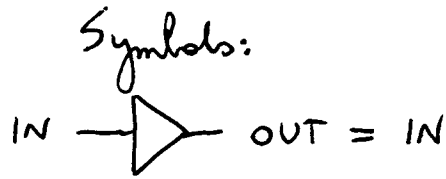
— Digital circuits

→ operate on binary logic $\left\{ \begin{array}{l} "0" \text{ is GND} \\ "1" \text{ is } V_{CC} (V_{DD}) \text{ typ. } 5V \\ \text{positive power supply or lower} \end{array} \right.$

→ allow simple (switched) control of analog functions, and processing of digitized signals prior to display, logging, or transmission.

Logic "gates":

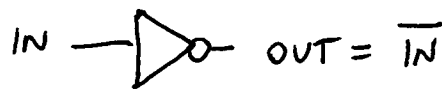
- BUFFER (digital):



Truth tables:

IN	OUT
0	0
1	1

- INVERTER (digital):

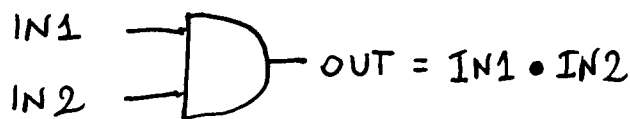


IN	OUT
0	1
1	0

In general, the circle at the output or input of a gate denotes signal inversion.

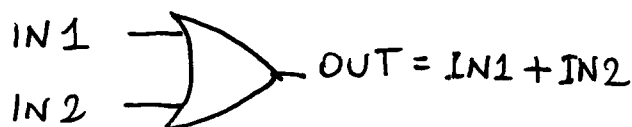
$IN \rightarrow \text{circle} \rightarrow \text{triangle} \rightarrow OUT = \overline{IN}$ is also an inverter.

- AND gate:




IN1	IN2	OUT
0	0	0
0	1	0
1	0	0
1	1	1

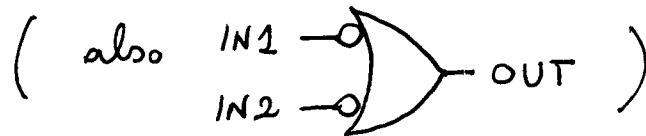
- OR gate:

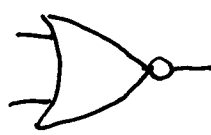


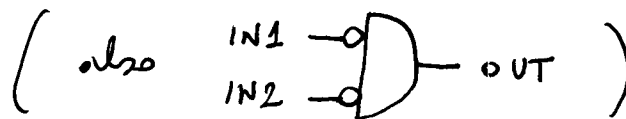
IN1	IN2	OUT
0	0	0
0	1	1
1	0	1
1	1	1

Composite gates :

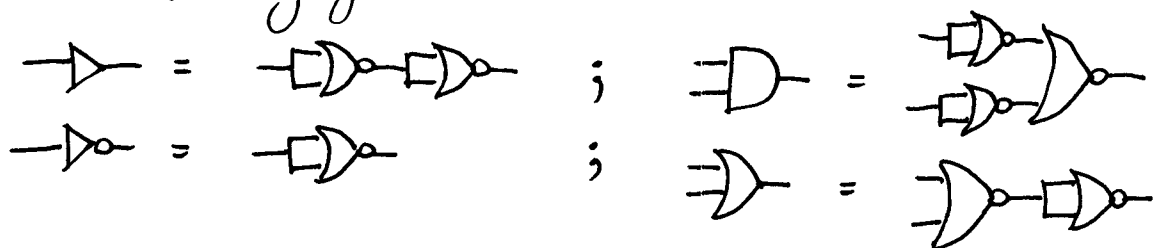
- NAND (NOT AND) :  $OUT = \overline{IN1 \cdot IN2}$
 $= \overline{IN1} + \overline{IN2}$



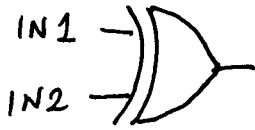
- NOR (NOT OR) :  $OUT = \overline{IN1 + IN2}$
 $= \overline{IN1} \cdot \overline{IN2}$



NOTE : NAND and NOR are considered fundamental building blocks of digital logic, and are more commonly used than AND and OR in constructing logic, because they are UNIVERSAL, e.g. for NOR:



Field programmable gate arrays (FPGAs) typically use arrays of NOR and NAND gates to synthesize programmable logic functions.

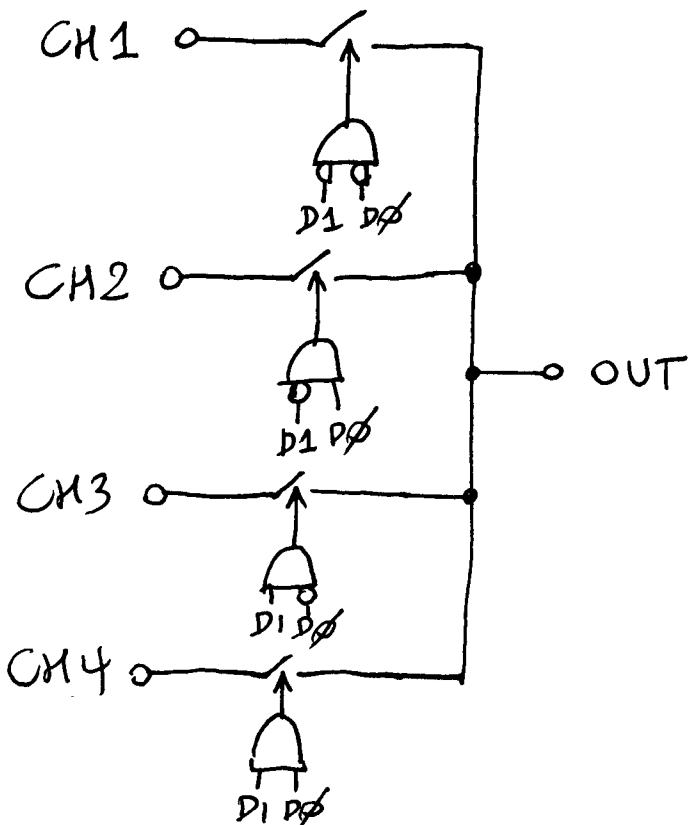
- XOR (exclusive-OR) :  $OUT = IN1 \oplus IN2$
 $= IN1 \cdot \overline{IN2} + \overline{IN1} \cdot IN2$

Flags when two binary values differ

IN1	IN2	OUT
0	0	0
0	1	1
1	0	1
1	1	0

- SUM, CARRY, etc \rightarrow digital arithmetic

Example : Analog multiplexer : digital control for selection of one out of several input "channels":
 e.g. 4 channels \rightarrow 2 selection bits
 CH1 .. CH4
 D1, D0
 MSB LSB



D1	D0	OUT connects to:
0	0	CH1
0	1	CH2
1	0	CH3
1	1	CH4

Useful, for instance, to select between leads in multi-electrode ECG.