

VLSI Implementation of the Pacemaker Unit of the Interstitial Cell of Cajal

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Abstract

The digestion of the food in the gastro-intestinal tract is aided by the peristaltic contractions of the gastric muscles. This gastric motility is a result of the spontaneous rhythmic pacemaker activity produced by the interstitial cells of Cajal (ICC), which line the gastro-enteric system. The interstitial cells of Cajal are a specialized group of neuro-muscular cells and are derived from fibroblasts. These cells generate periodic action potentials termed as slow waves, which are responsible for gastric motility. The objective of this project is to implement a VLSI model of a simple ICC network capable of producing slow waves generated by the ICC network of the stomach. The cells of the network are designed using a mathematical model where the membrane voltage of the ICC is based on the flow of Ca^{2+} ions and Na^{+} ions.

1 Introduction:

The human digestive system has the tasks of ingestion, digestion, absorption and assimilation of food. The food taken in is pushed through the alimentary canal by a series of rhythmic contractions of the smooth muscles lining the gastro-intestinal (GI) tract called peristalsis. These contractions are caused by a set of electrical signals called "slow waves". The slow-waves, in turn, are generated by the Interstitial cells of Cajal which also line the GI tract.

The slow waves are a summation of a large number of various functional cell membrane fluctuations called "Unitary Potentials (UP)". The unitary potentials are generated from a group of cell organelles called "Pacemaker Unit (PU)". The UP is generated by the flow of Ca^{2+} ions through the Pacemaker Unit.

Abnormalities in the Interstitial Cells of Cajal could result in gastric diseases like Irritable Bowel Syndrome and Pylorus Dysfunction. In this project, a VLSI model of the Pacemaker Unit, which is the most fundamental unit of the ICC, is built using VHDL from a proven biophysical model.

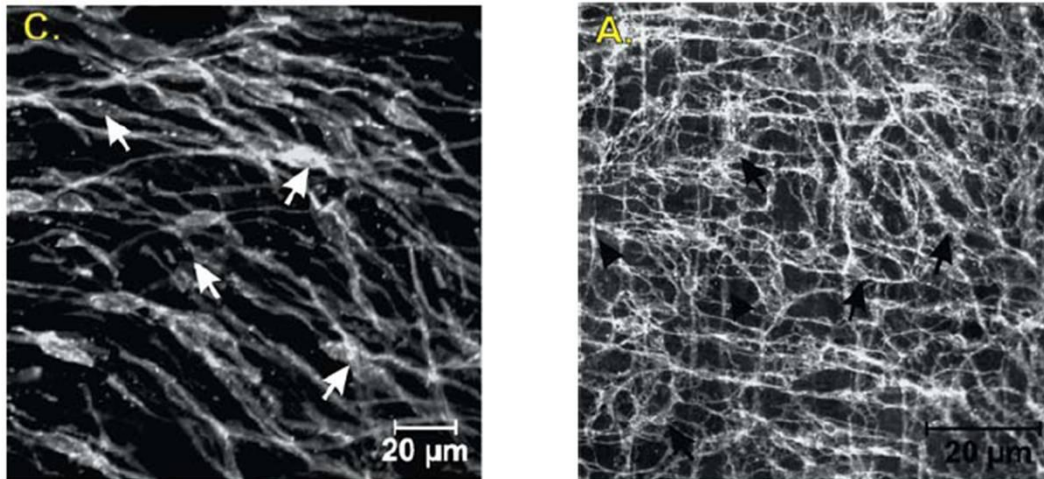
2 Biophysical Background:

2.1 The Interstitial Cell of Cajal:

The Interstitial Cells of Cajal were first isolated by Santiago Ramon y Cajal. These cells are found along the entire gut wall including the myenteric plexus and at the interface between the circular muscle and the submucosa. These cells are neither neurons nor muscular cells

43 and are supposed to be derived from fibroblasts. The ICC are electrically coupled to the
44 enteric muscle cells through gap junctions. The slow waves in the digestive system are
45 generated by a large group of these cells.

46 Each part of the digestive system has its own characteristic slow-wave. For example, in the
47 human digestive system, the frequency of the slow-waves is 3 cycles per minute in the
48 stomach and 12 cycles per minute in the duodenum. This variation is largely attributed to the
49 difference in the ICC population in the various digestive organs. Figure 1 shows the different
50 population of the ICC in the rat stomach and the rat intestine.



51

52

Figure 1: ICC distribution along the murine stomach and murine intestine[2]

53

54 2.2 The Pacemaker Unit:

55 [2] suggests that the Interstitial Cell of Cajal is fundamentally made up of a number of small
56 functional units which are responsible for the generation of the slow waves. These units are
57 called the pacemaker units and essentially are made up of four components:

58 2.2.1 The Endoplasmic Reticulum(ER):

59 It is the intracellular Ca^{2+} store that cycles Ca^{2+} by release via the IP_3R and is sequestered
60 back again by the sarcoendoplasmic reticulum calcium ATPase (SERCA) pump proteins.

61 2.2.2 The Mitochondrial Subspace (MT) :

62

63 It regulates the cellular ATP production through the mitochondrial calcium uni-
64 porter(MCU) and the Mitochondrial Sodium/Calcium Exchanger(NCX).

65

66 2.2.3 Cytosolic Subspace(S_1 and S_2):

67

68 These two form the remaining of the pacemaker unit and includes the Non-Selective
69 Cation conductance exchanger(NSCC) and the intracellular Ca^{2+} fluxes(S_1S_2).

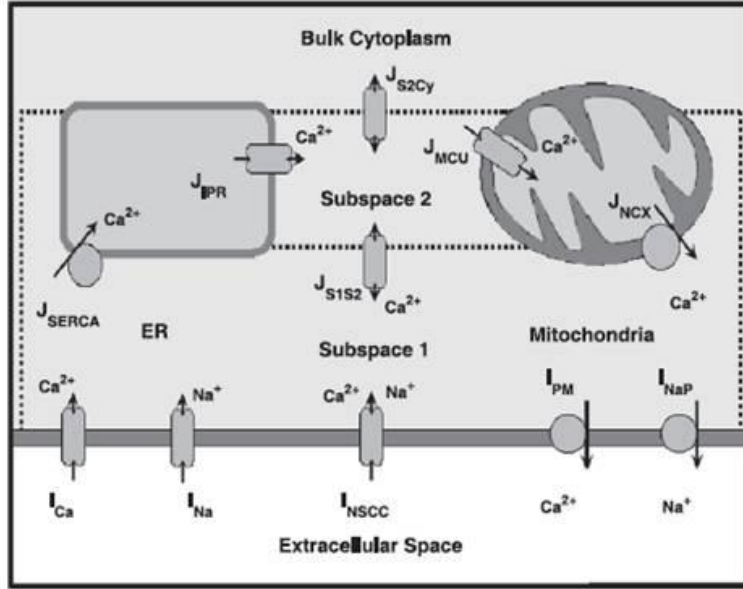
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71 2.3 The Unitary Potential:

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73 The Unitary Potential is generated in the Pacemaker Unit as a consequence of the flow of
74 Ca^{2+} ions. Initially Ca^{2+} ions flow into the S_1 subspace which then diffuse to S_2
75 .Sufficient Ca^{2+} entry into S_2 raises the IP_3R open probability causing a flow of Ca^{2+}
76 from the Endoplasmic Reticulum. The mitochondria also gets activated through the MCU
77 channel, causing rapid mitochondrial Ca^{2+} accumulation. To maintain ionic concentrations
78 in the ER, the ER takes up Ca^{2+} ions through the SERCA pump. The deficiency in the ions
79 in S_1 causes the NSCC channel to open up taking up both Na^+ and Ca^{2+} ions. This
80 depolarization is then followed by a repolarization where mitochondria releases the excess

81 Ca^{2+} ions through NCX and S_1 releases Na^+ ions into the extracellular space. This
 82 process is cyclic and gives rise to a unitary potential cycle.
 83



84 Figure 2: The schematic diagram of the Pacemaker Unit and the flow of ions.
 85
 86

87 2.4 The Model Framework:

88
 89 [2] models the Unitary Potential as a state model of 5 differential equations governing
 90 the basic parameters. The state variables are:

- 91 V_m : Membrane Potential
- 92 C_{S1} : Ca^{2+} concentration in S_1
- 93 C_{S2} : Ca^{2+} concentration in S_2
- 94 C_{ER} : Ca^{2+} concentration in ER
- 95 C_{MT} : Ca^{2+} concentration in MT
- 96 N_{S1} : Na^+ concentration in S_1
- 97 H: opening gate variable
- 98 Φ_3 : IP_3R slow variable

99 The state equations are given by:

$$100 \frac{dV_m}{dt} = -\frac{1}{C_m} (I_{iNa} + I_{iCa})$$

$$101 \frac{dC_{S1}}{dt} = J_{S1S2} + \lambda_{MT/S_1} J_{NCX} - \left(\frac{\delta_S(\text{PU})}{V_{Scale} Z_{Ca}} \right) I_{iCa} - \lambda_{ER/S_1} J_{SERCA}$$

$$102 \frac{dC_{S2}}{dt} = J_{S2Cy} + \lambda_{ER/S_2} J_{IPR} - \lambda_{S_1/S_2} J_{S1S2} - \lambda_{MT/S_2} J_{MCU}$$

$$\frac{dC_{ER}}{dt} = J_{SERCA} - J_{IPR}$$

$$\frac{dC_{MT}}{dt} = f_m (J_{MCU} - J_{NCX})$$

$$\frac{dN_{S1}}{dt} = - \left(\frac{\delta_S(\text{PU})}{V_{Scale} Z_{Na}} \right) I_{iNa}$$

$$\frac{dH}{dt} = \phi_3 (1 - H) - \left(\frac{P \phi_1 \phi_2}{P \phi_1 + \phi_{-1}} \right) H$$

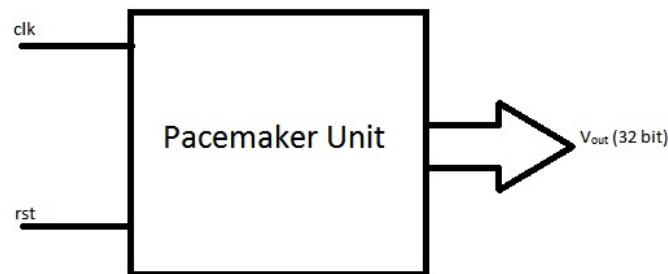
104 Where the J_i is the Ca^{2+} flux due to the particular channel i , ϕ_1 and ϕ_2 are the opening and
105 closing gate variables of IP_3R and f_m is the mitochondrial buffering rate.

106

107 3. System Implementation:

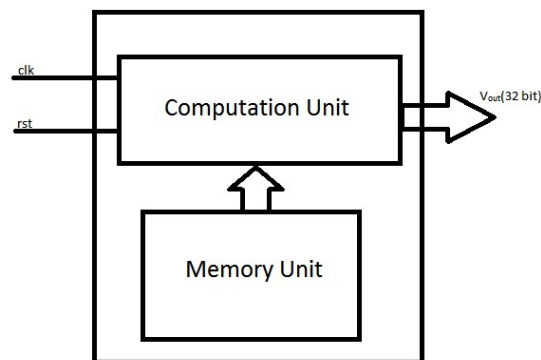
108 3.1 Basic Block Diagram:

109 The Pacemaker Unit's digital VLSI model has two inputs viz. the Clock and the Reset
110 and a 32 bit output for the output voltage generated. This is as shown in Figure 3



111

112 Figure 3: Black Box of Pacemaker Unit



113

114 Figure 4: Block Diagram of the Pacemaker Unit

115

116 The Pacemaker Unit's block diagram is shown in the following diagram. The constants
117 and the parameters are stored in a memory block in the 32 bit IEEE-754 format. The main
118 advantage of this format is that floating point numbers are easy to represent and compute.
119 The membrane voltage and the other state parameters are calculated in the computation
120 block. The system is a positive edge triggered system and consists of 32 bit floating point
121 multipliers, adders and subtractors.

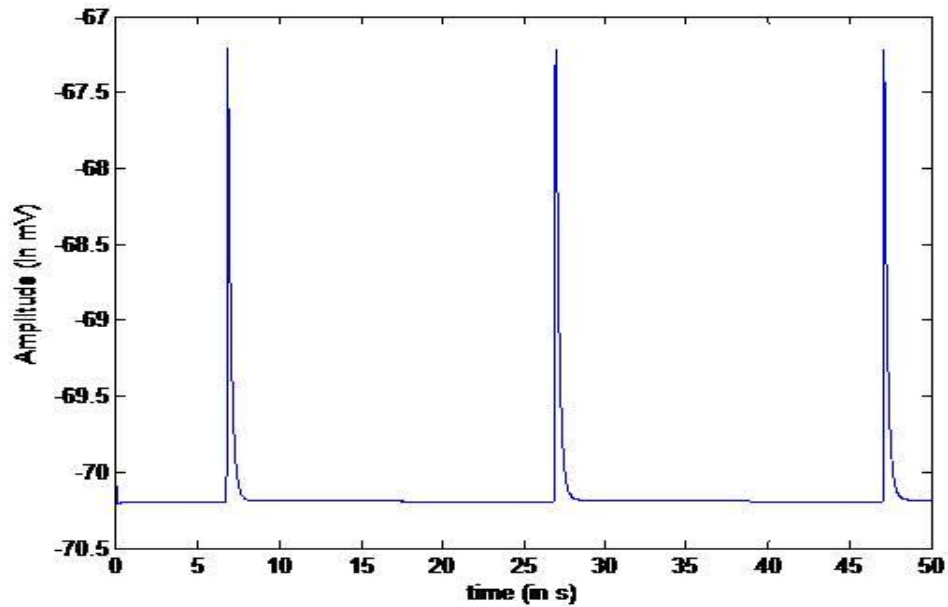
122 To verify the accuracy of the model, the system was first simulated on MATLAB with a
123 initial resting potential of -70.1 mV. The system was also simulated in MATLAB to
124 determine the clock frequency required to run the system so as to obtain a unitary potential
125 of 3 cycles/minute as the case with most mammals.

126 The actual model was simulated using VHDL on Altera's FPGA software Quartus II. The
127 output waveforms were analyzed using ModelSim and the Register Transfer Level (RTL)
128 schematic was obtained.

129

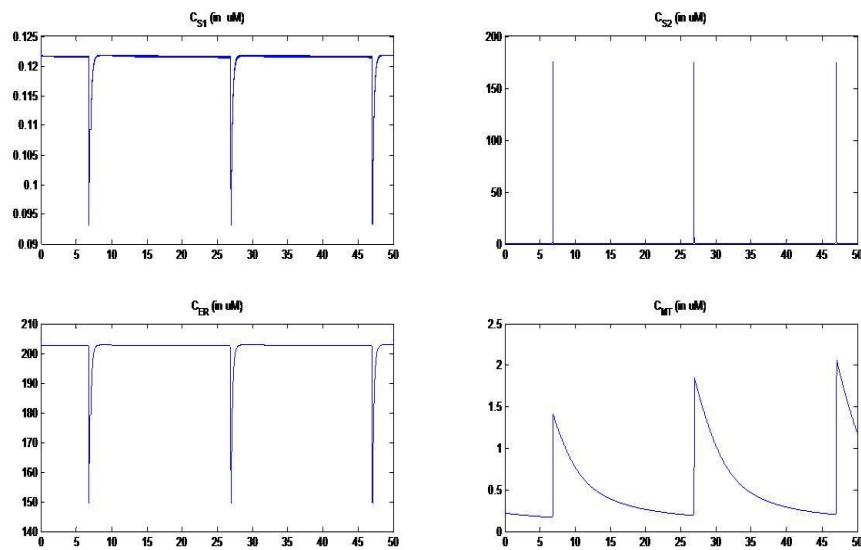
130 **4. Results:**

131 Figure 5 shows the MATLAB simulation of the system using MATLAB's ode23 solver. By a
132 hit-and-trial method, the system was found to generate a unitary potential of the desired
133 frequency when the samples were spaced at 1.54 ms. Thus it was decided that the clock
134 frequency of the system to be at 6.4 kHz. Figure 6 shows the various Ca^{2+} concentrations
135 across the different parts of the Pacemaker Unit.



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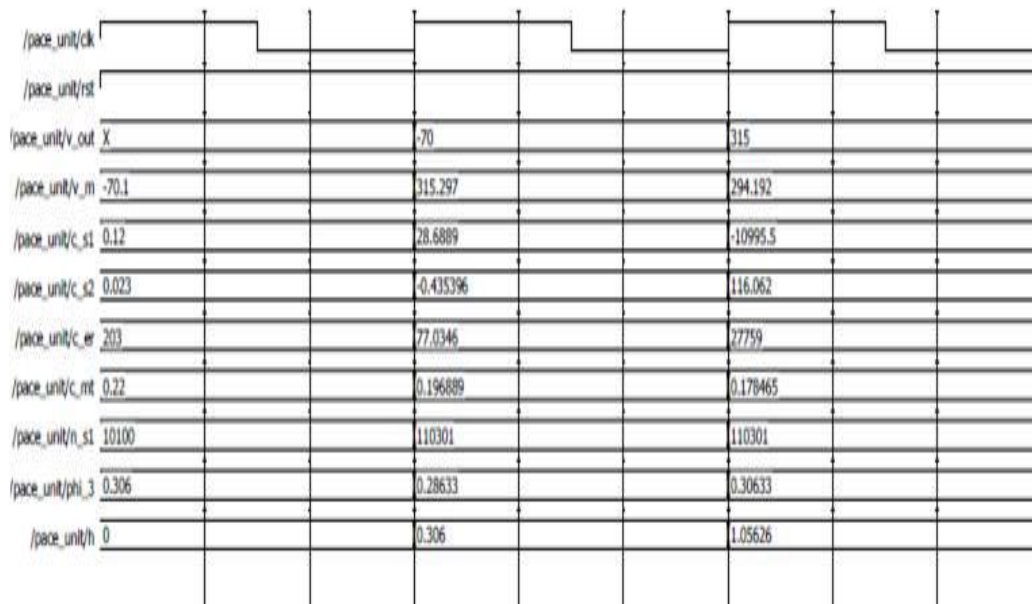
Figure 5: MATLAB: Unitary Potentials (Amplitude 3 mV pk-pk)



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Figure 6: MATLAB Ca^{2+} ion flow in various components of the Pacemaker Unit

145 Figure 7 shows the waveform simulation using VHDL at a clock of 6.4 kHz.
 146 The system was built using the behavioural model and employed the Euler's
 147 method for solving the differential equations. Appendix A shows the RTL
 148 schematic synthesized for the Pacemaker Unit.



149
 150 Figure 7: VHDL Simulation Output of the Pacemaker Unit
 151

152 5. Conclusion and Future Work:

153 Thus the VLSI model of the Pacemaker Unit was obtained using VHDL and
 154 verified with MATLAB simulations. The Interstitial Cell of Cajal has more
 155 than one Pacemaker Unit. Hence the collective summation of all the
 156 Pacemaker units has to be studied. Also the gastric wall is lined with more
 157 than one ICC. Hence it is necessary to study the effects of many ICCs and
 158 the effect of the ICC population on the characteristics of the slow wave
 159 generated.

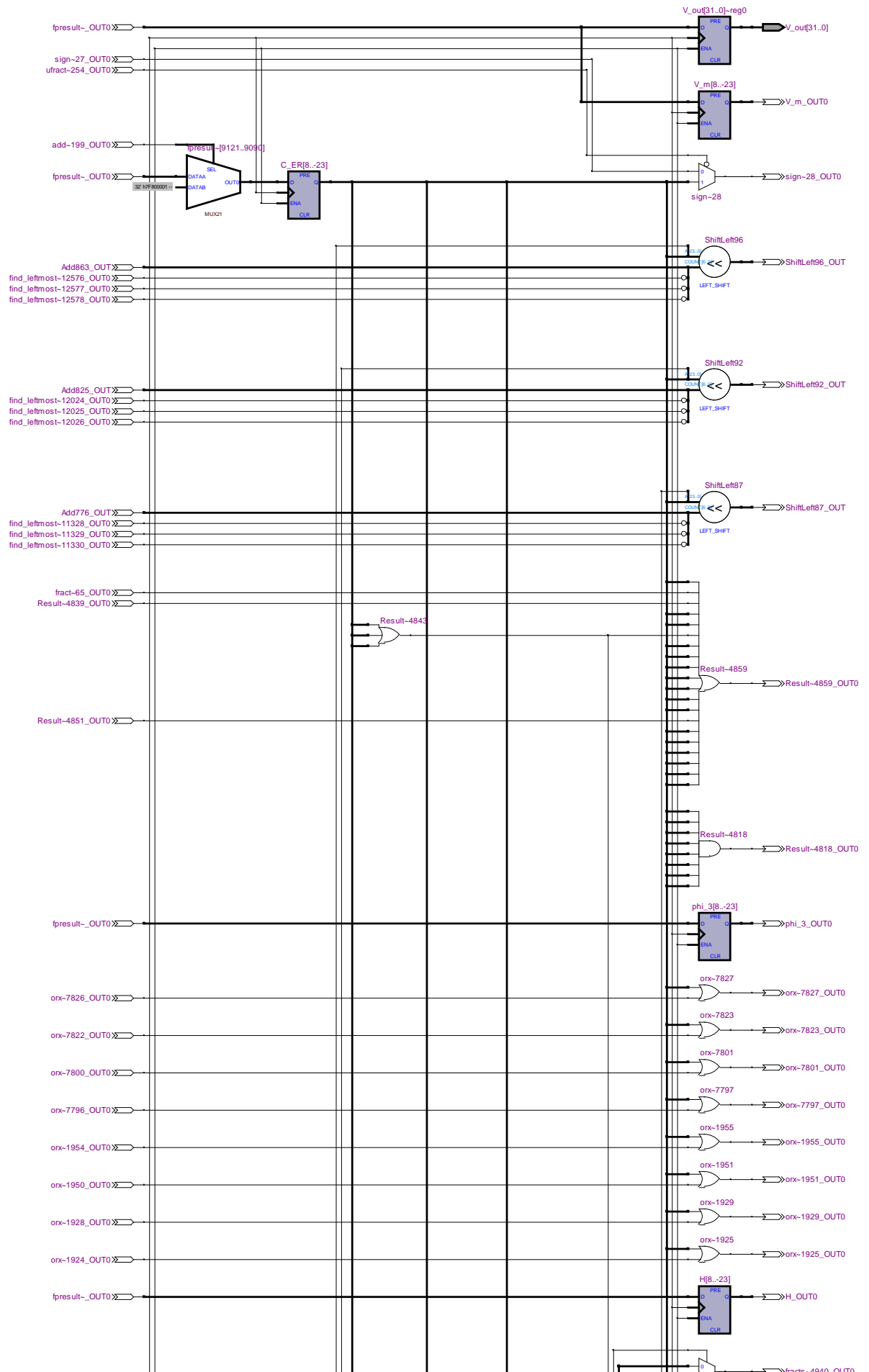
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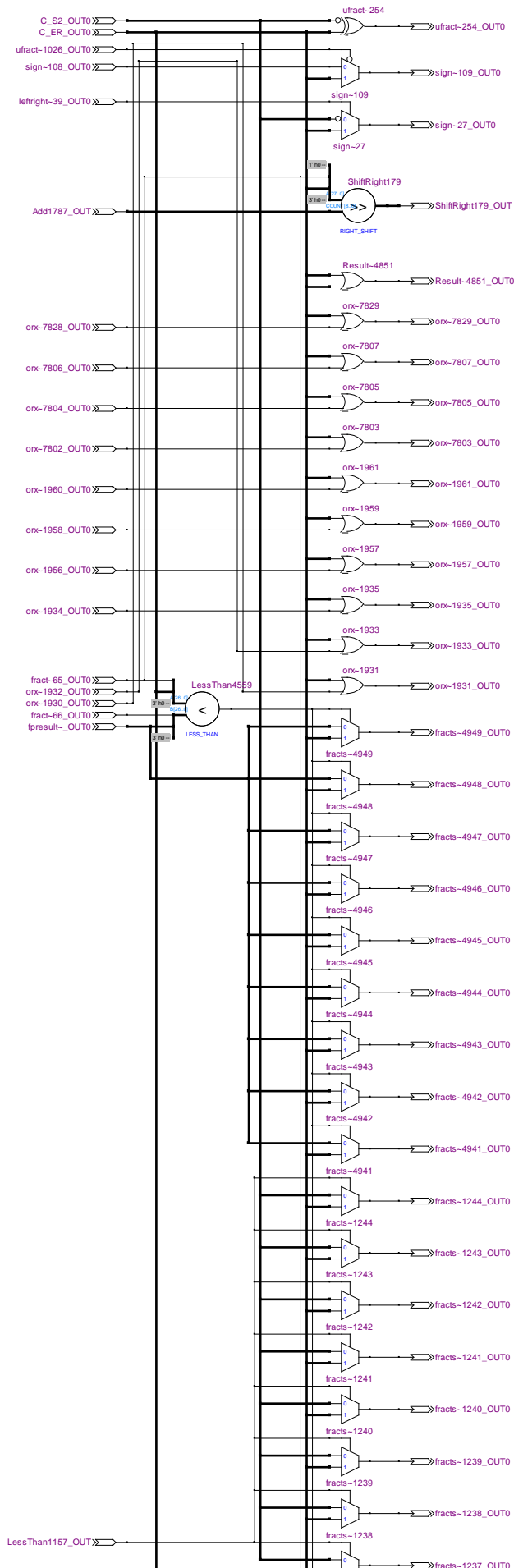
- 161 [1] Sanders, K.M., T. Koh, S.D. and Ward., S.M., "Interstitial Cells of Cajal as pacemakers in
 162 the gastrointestinal tract", Annu Rev. Physiol. 68:307-343.
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 164 [2] Faville, R. , A. Pullan, K. Sanders and N. Smith.2008. A biophysically based mathematical model of
 165 unitary potential activity in interstitial cells of Cajal."Biophysical Journal 95(1):88-104.
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 167 [3] Douglas L. Perry, VHDL- Programming by Example,McGraw-Hill
 168 Publishers.

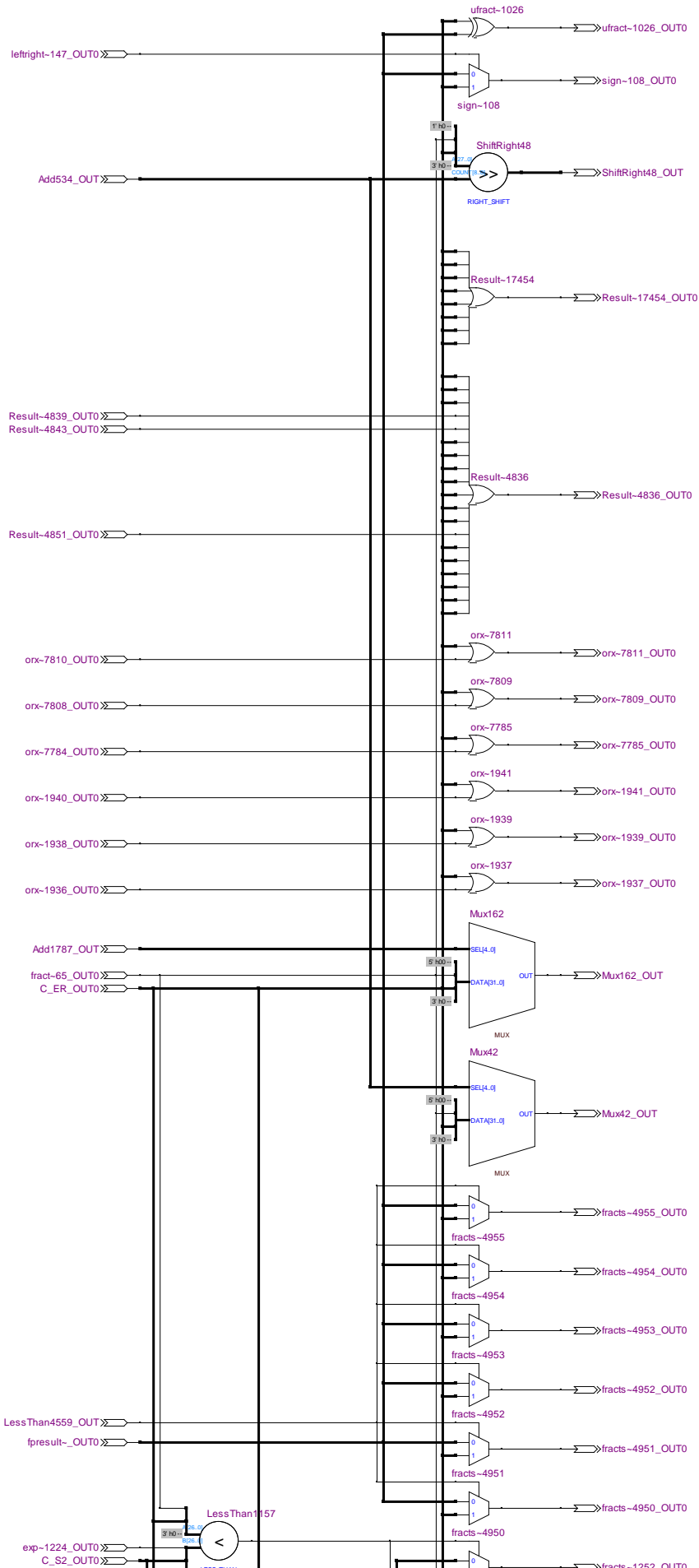
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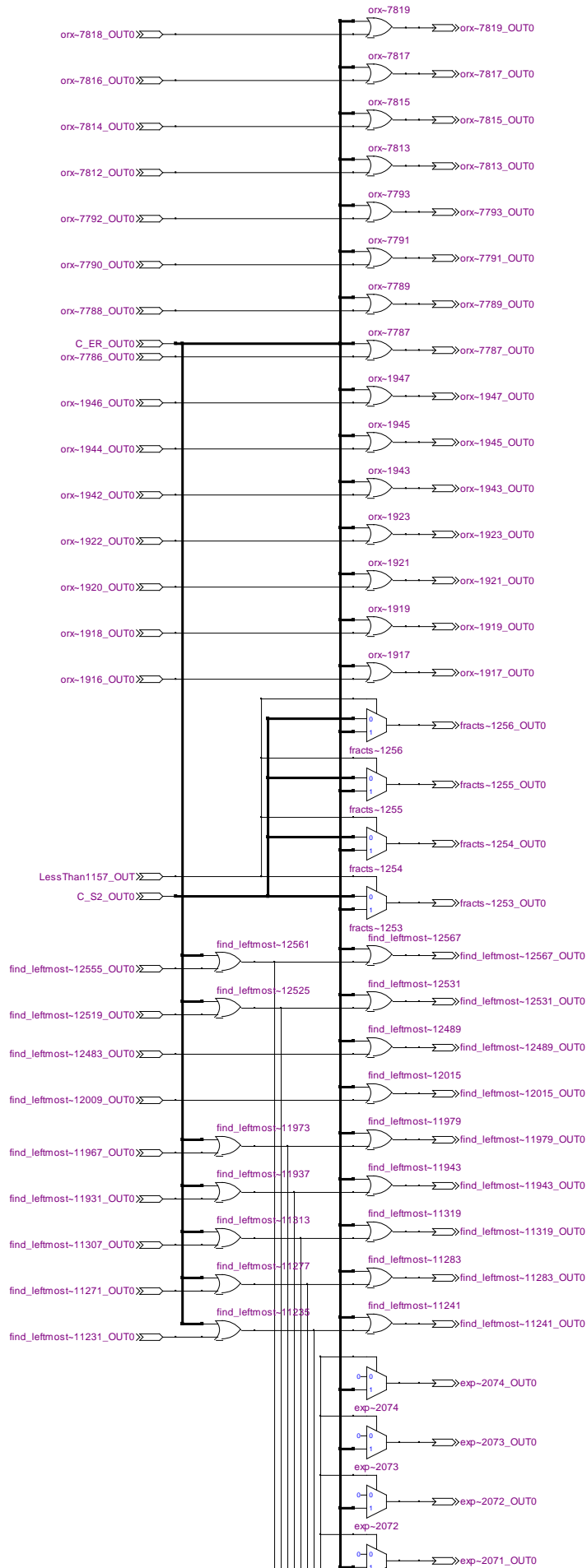
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Appendix A
RTL Schematic of the Pacemaker Unit

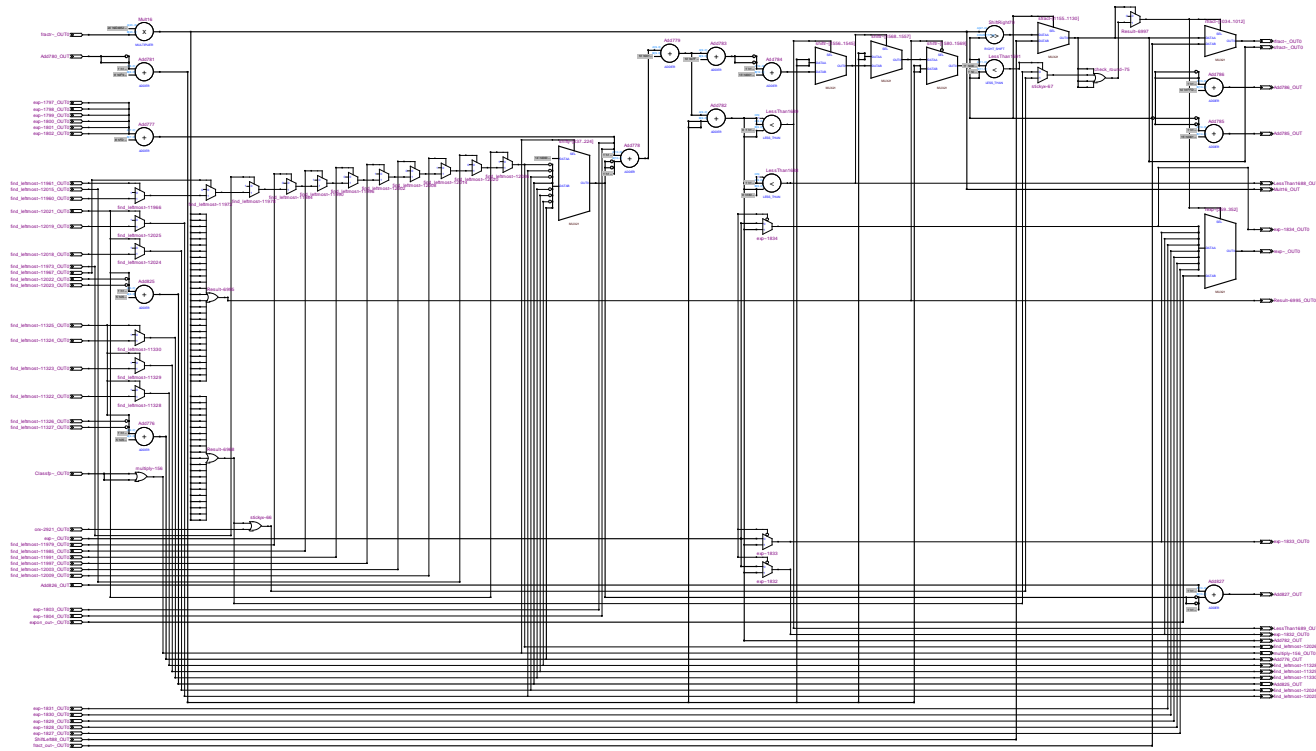




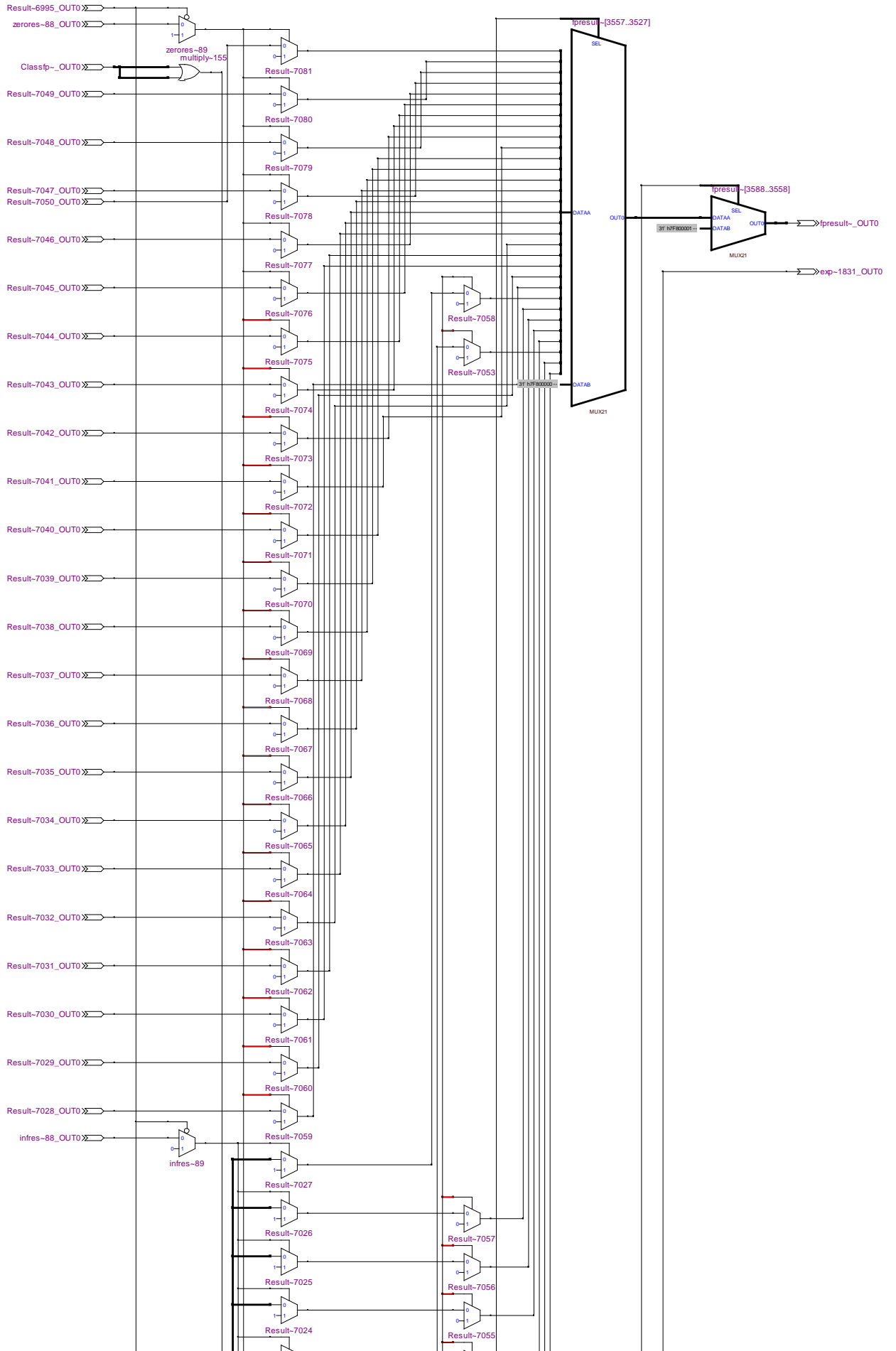


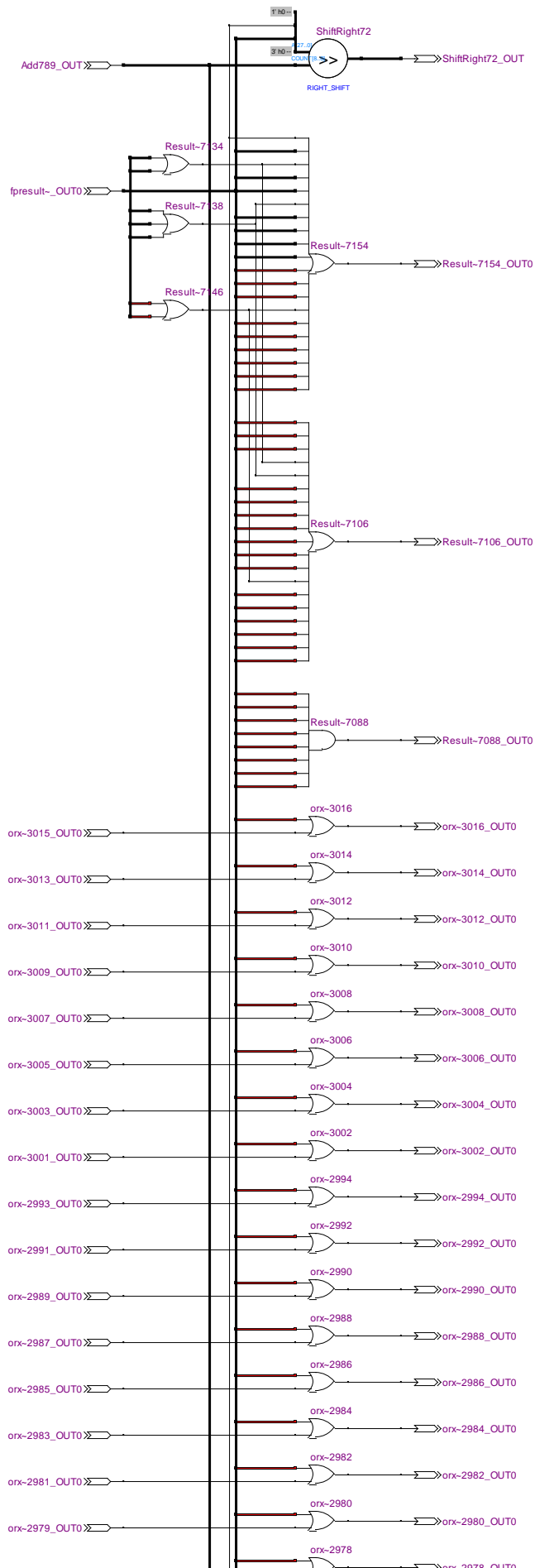


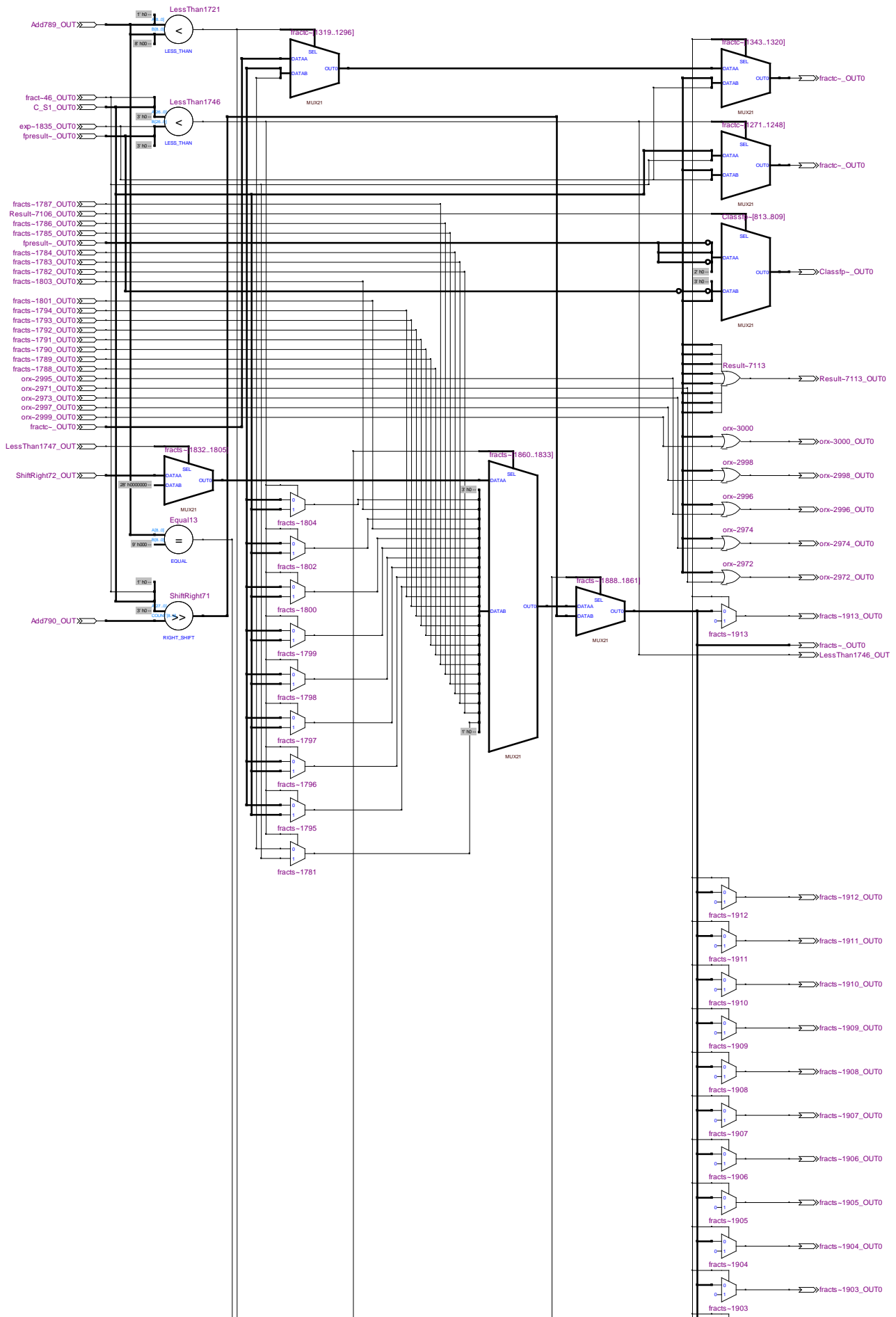
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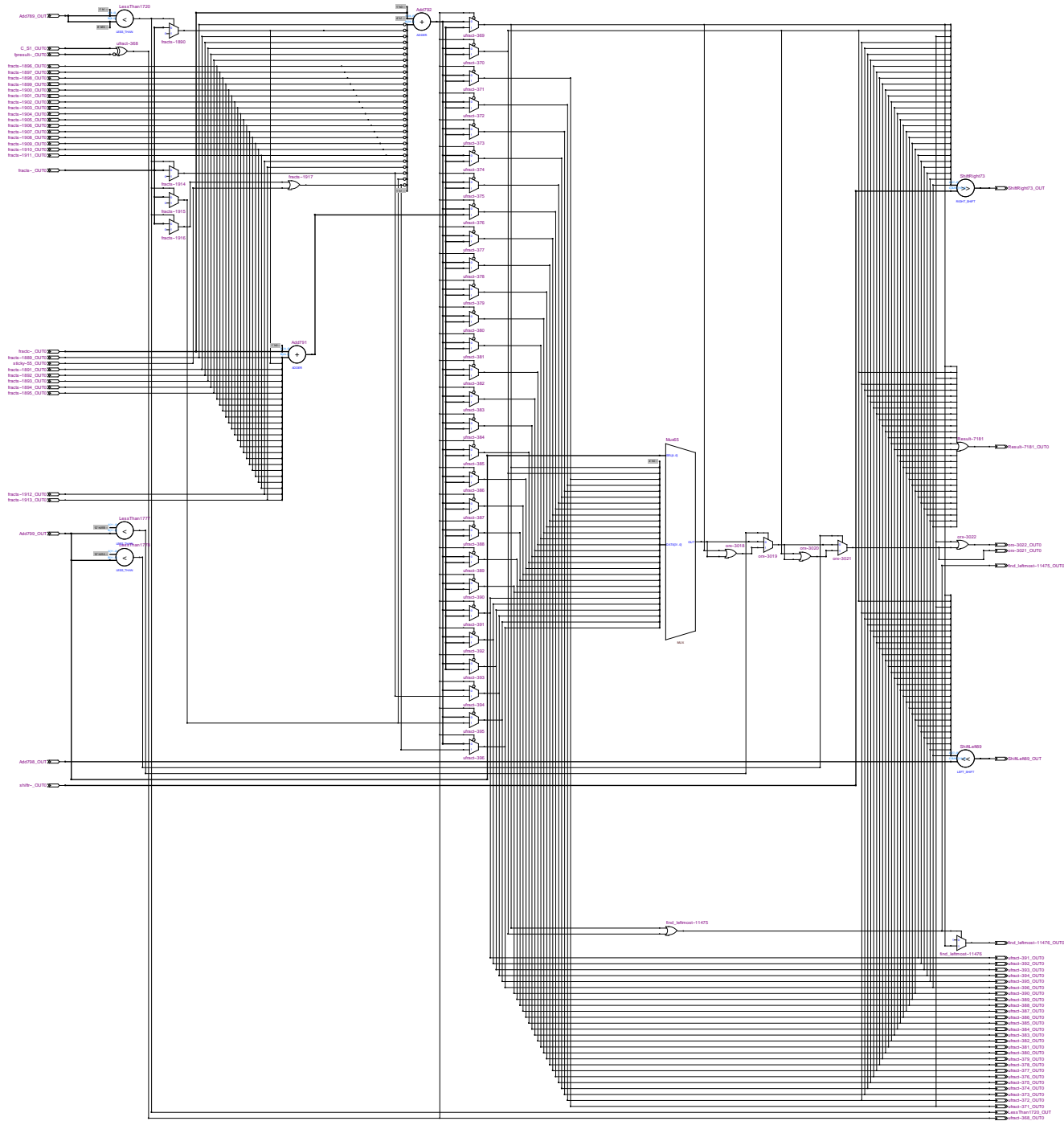


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Appendix B

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VHDL Code for the Pacemaker Unit

215

```
library IEEE;
```

216

```
use IEEE.std_logic_1164.all;
```

217

```
use IEEE.std_logic_arith.all;
```

218

```
use IEEE.math_real.all;
```

219

```
--library IEEE_PROPOSED;
```

220

```
--use IEEE_PROPOSED.fixed_float_types.all;
```

221

```
--use IEEE_PROPOSED.fixed_pkg.all;
```

222

```
--use IEEE_PROPOSED.float_pkg.all;
```

223

224

```
entity Pace_Unit is
```

225

```
    port (clk,rst:in STD_LOGIC;V_out:out STD_LOGIC_VECTOR(31 downto 0));
```

226

227

```
        end Pace_Unit;
```

228

```
architecture PU of Pace_Unit is
```

229

```
-- UP Model Parameters
```

230

```
constant g_Ca : real := 0.01;
```

231

```
constant E_NSCC : real := 0.0;
```

232

```
constant g_capNSCC_Ca : real := 0.12;
```

233

```
constant g_capNSCC_Na :real := 220.0;
```

234

```
constant K_NSCC :real := 0.12;
```

235

```
constant h_NSCC :real := 3.0;
```

236

```
constant g_PM :real := 420.0;
```

237

```
constant K_PM :real := 1.0;
```

238

```
constant g_Na :real := 15000.0;
```

239

```
constant K_Na :real := 10000.0;
```

240

```
constant h_Na :real := 4.0;
```

241

```
constant V_SERCA :real := 100000.0;
```

242

```
constant A_2 :real := 0.0006;
```

243

```
constant A_4 :real := 3.57;
```

244

```
constant A_5 :real := 0.000027;
```

245

```
constant A_6 :real := 0.0000231;
```

246

```
constant V_MCU :real := 800.0;
```

247

```
constant K_MCU :real := 10.0;
```

248

```
constant K_INH :real := 10.0;
```

249

```
constant h_INH :real := 4.0;
```

250

```
constant V_NCX :real := 0.5;
```

251

```
constant K_NCX :real := 0.3;
```

252

```
constant u_S1S2 :real := 0.04;
```

253

```
constant k_IPR :real := 2000.0;
```

254

```
constant k_1 :real := 0.0;
```

255

```
constant k_min1 :real := 6.4;
```

256

```
constant k_2 :real := 4.0;
```

257

```
constant r_2 :real := 200.0;
```

258

```
constant r_min2 :real := 0.0;
```

259

```
constant r_4 :real := 750.0;
```

260

```
constant R_1 :real := 36.0;
```

261

```
constant R_3 :real := 300.0;
```

262

```
constant g_alpha :real := 0.02;
```

263

```
constant g_beta :real := 300.0;
```

264

```
constant K_beta :real :=2.0;
```

265

```
constant h_beta :real := 2.0;
```

266

```
constant K_m :real := 0.01;
```

267

```
constant B_m :real := 100.0;
```

```

268 constant y_S1 :real := 100.0;
269 constant y_S2 :real := 1.0;
270 constant y_ER :real := 20.0;
271 constant y_MT :real := 200.0;
272 constant d_S :real := 26.0;
273 constant C_m :real := 20.0;
274 constant Z_Ca :real := 2.0;
275 constant Z_Na :real :=1.0;
276 constant V_t :real := 26.7;
277 constant C_O :real:= 1800.0;
278 constant P :real := 1.0;
279 signal V_m :real := -70.1;
280 signal C_S1 :real := 0.12;
281 signal C_S2 :real := 0.023;
282 signal C_ER :real := 203.0;
283 signal C_MT :real := 0.22;
284 signal N_S1 :real := 10100.0;
285 signal H : real := 0.0;
286 signal phi_3 :real := 0.306;
287 signal a_phi3,b_phi3,phi_1,phi_min1,phi_2,J_IPR,J_S1S2,J_NCX,J_MCU,J_SERCA : real := 0.0
288 ;
289 signal
290 I_Na,I_PM,g_NSCC_Ca,g_NSCC_Na,I_NSCC_Ca,I_NSCC_Na,E_Ca,I_Ca,I_iCa,I_iNa,f_m :
291 real := 0.0 ;
292 signal l_MTS1,l_ERS1,l_ERS2,l_S1S2,l_MTS2 : real := 0.0 ;
293 begin
294     process(clk,rst)
295     begin
296         if rst = '1' and rising_edge(clk) then
297             V_out <= CONV_STD_LOGIC_VECTOR(INTEGER(V_m),32);
298             a_phi3 <= g_alpha;
299             b_phi3 <= g_beta*((C_S2**h_beta)/(K_beta**h_beta+C_S2**h_beta));
300             phi_3 <= phi_3+ (a_phi3-b_phi3*phi_3);--IP3R Slow Rate Variable
301             --IP3R Constants
302             phi_1 <= (k_1*R_1+r_2*C_S2)/(R_1+C_S2);
303             phi_min1 <= ((k_min1+r_min2)*R_3)/(R_3+C_S2);
304             phi_2 <= (k_2*R_3+r_4*C_S2)/(R_3+C_S2);
305             J_IPR <=k_IPR*(((P*phi_1*H)/(P*phi_1+phi_min1))**4.0)*(C_ER-C_S2);
306             J_S1S2 <= u_S1S2*(C_S2-C_S1);
307             J_NCX <= V_NCX*(C_MT/(K_NCX+C_MT));
308             J_MCU <= V_MCU*((C_S2**2.0)/(K_MCU**2.0+C_S2**2.0));
309             J_SERCA <= V_SERCA*((C_S1-A_2*C_ER)/(1.0
310 +A_4*C_S1+A_5*C_ER+A_6*C_S1*C_ER));
311             I_Na <= g_PM*(C_S1**h_Na/(K_Na**h_Na+C_S1**h_Na));
312             g_NSCC_Ca <=
313 g_capNSCC_Ca*(K_NSCC**h_NSCC/(K_NSCC**h_NSCC+C_S1**h_NSCC));
314             g_NSCC_Na <=
315 g_capNSCC_Na*(K_NSCC**h_NSCC/(K_NSCC**h_NSCC+C_S1**h_NSCC));
316             I_NSCC_Ca <= g_NSCC_Ca*(V_m-E_NSCC);
317             I_NSCC_Na <= g_NSCC_Na*(V_m-E_NSCC);
318             E_Ca <= 0.5*V_t*log(C_O/C_S1);
319             I_Ca <= g_Ca*(V_m-E_Ca);
320             l_MTS1 <= y_MT/y_S1;
321             l_ERS1 <= y_ER/y_S1;
322             l_ERS2 <= y_ER/y_S2;
323             l_S1S2 <= y_S1/y_S2;

```

```

324         l_MTS2 <= y_MT/y_S2;
325         f_m <= 1.0/(1.0+(K_m*B_m/(K_m+C_MT**2.0)));
326         I_iNa <= I_NSCC_Na+I_Na;
327         I_iCa <= I_NSCC_Ca+I_Ca;
328         V_m <= V_m- ((I_iCa+I_iNa)/C_m);
329         C_S1 <= C_S1 + (J_S1S2+l_MTS1*J_NCX)-
330 ((d_S/Z_Ca)*I_iCa+l_ERS1*J_SERCA);
331         C_S2 <= C_S2 + (l_ERS2*J_IPR-(l_S1S2*J_S1S2+l_MTS2*J_MCU));
332         C_ER <= C_ER + (J_SERCA-J_IPR);
333         C_MT <= C_MT + f_m*(J_MCU-J_NCX);
334         N_S1 <= N_S1 - ((d_S/Z_Na)*I_iNa);
335         H <= H+ ((phi_3*(1.0-H))- (((P*phi_1*phi_2)/(P*phi_1+phi_min1)*H)));
336         --V_out <= CONV_STD_LOGIC_VECTOR(INTEGER(V_m),32);
337
338
339         end if;
340     end process;
341 end PU;
342
343
344
345
346

```