• Open book, open notes. *It will be helpful to review the material covered in homework 1 through 4.* You do not need access to Cadence, Matlab, or other computational tool to complete this midterm.

• Take the midterm wherever and whenever is most convenient to you. No communication except with the instructor and TAs.

• Submit a single PDF file with all your solutions by 11:59pm on the due date on Canvas/Gradescope.

1. Project proposal [20 points].
   Identify a topic and formulate a proposal for a potential design project in this course. No diagrams or equations are necessary; just list the title of a proposed project for the full-custom design of a neuromorphic or bioelectronic integrated circuit and a brief (500 words or less) paragraph of text describing the problem that your proposed circuit addresses, the objective(s) to be met in the design, and your proposed approach to achieve the objective(s).

   If you have already formed a group and are proceeding with your final project, your proposal may be closely related, but formulate your project in your own words and no not copy or communicate material with your group mates. If you are not part of a group or haven’t yet formulated a project, this is your opportunity to express what you would like to get out of the design experience in this course culminating in the final project.

2. Ion channel conductance [20 points].
   (a) [10 points] Consider an nMOS transistor with source connected to $E_K$, modeling a potassium ion channel with reversal potential $E_K$. Both the drain and source connect to the membrane. Find the subthreshold slope of the small-signal membrane conductance $g_m = dI_K / dV_m$ as a function of the membrane voltage $V_m$ for $\kappa_n = 0.7$ at room temperature, and compare with a typical subthreshold slope for a biophysical potassium ion channel conductance.

   (b) [10 points] How would you change the circuit to implement a more biophysically realistic model of a slow activation potassium ion channel?

3. Silicon retina active pixel sensor [30 points].
   Consider the active pixel circuit shown in the diagram below. The pixel is activated by a logic high voltage on the SEL row select line, producing an output voltage $V_{out}$ measured on the output column line in response to light illuminating the pixel generating a photocurrent $I_{photo}$. 
(a) [20 points] Show that the output voltage $V_{\text{out}}$ measured when the activated pixel is illuminated at an intensity generating a photocurrent $I_{\text{photo}}$ is given by

$$V_{\text{out}} = V_{\text{out, ref}} - \frac{V_t}{\kappa_{\text{in}}} \ln \left( \frac{I_{\text{photo}}}{I_{\text{photo, ref}}} \right)$$

where $V_{\text{out, ref}}$ is the reference output voltage measured when the pixel is illuminated at a reference intensity generating a reference photocurrent $I_{\text{photo, ref}}$.

(b) [10 points] How is the output affected by transistor mismatch caused by imprecision in the fabrication process? How is it affected by variations in temperature? Explain.

4. *Gm-C lowpass filter* [30 points].
   (a) [10 points] Consider the Gm-C first-order lowpass filter circuit shown to the right. Draw the transistor-level circuit schematic of a differential-input, single-ended output operational transconductance amplifier (OTA) that implements the Gm cell with a bias current $I_b$ as shown.

   (b) [10 points] Using your OTA design, find the DC gain and the cut-off frequency of the lowpass filter.

   (c) [10 points] Estimate the power consumption of the lowpass filter using your design. What is the ratio of the power over the bandwidth? Interpret what you find.